## Math 819 HW 3- Due Thursday November 12

1. Let $\lambda=(3,2)$ and consider the Specht module $S^{\lambda}$ for $\Sigma_{5}$.
a. Find the dimension of $S^{\lambda}$.
b. Determine the basis of standard polytabloids.
c. Determine the matrices for the permutations $(1,2)$ and $(1,2,3,4,5)$ in terms of this basis.
d. Compute the Gram matrix for the usual bilinear form in terms of this basis.
e. Compute the dimension of the simple module $D^{\lambda}$ in characteristics 2 and 3 by determining the rank of the Gram matrix.
f. Determine the weights of a G-Z basis of $S^{\lambda}$ using residue sequences.
2. Page $65 \# 3$.
3. Page $70 \# 6$.
4. Page $83 \# 3$
5. Look over Green's Indecomposability Theorem and its proof on page 62.

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